Quantum Computer as Analog Computer on GPU

By Alexander Soiguine

Career Point University

Abstract- The geometric algebra lift of conventional quantum mechanics qubits is the game-changing quantum leap forward potentially kicking from the quantum computing market big fishes (IBM, Microsoft, Google, dozens of smaller ones) investing billions in elaborating quantum computing devices. It brings into reality a kind of physical field spreading through the whole three-dimensional space and values of the time parameter. The fields can be modified instantly in all points of space and time values. All measured observable values are simultaneously available all together, not through looking one by one. In this way the new type of quantum computer appeared to be a kind of analog computer keeping and instantly processing information by and on sets of objects possessing an infinite number of degrees of freedom. As practical implementation, the multithread GPUs with the CUDA language functionality allow creating of software simulating that kind of fields processing numbers of space/time discrete points only restricted by the GPU threads capacity.

GJSFR-F Classification: FOR Code: 0801

QUANTUMCOMPUTERASANALOGCOMPUTERONGPU

Strictly as per the compliance and regulations of:

Quantum Computer as Analog Computer on GPU

Alexander Soiguine[1]

Abstract- The geometric algebra lift of conventional quantum mechanics qubits is the game-changing quantum leap forward potentially kicking from the quantum computing market big fishes (IBM, Microsoft, Google, dozens of smaller ones) investing billions in elaborating quantum computing devices. It brings into reality a kind of physical field spreading through the whole three-dimensional space and values of the time parameter. The fields can be modified instantly in all points of space and time values. All measured observable values are simultaneously available all together, not through looking one by one. In this way the new type of quantum computer appeared to be a kind of analog computer keeping and instantly processing information by and on sets of objects possessing an infinite number of degrees of freedom. As practical implementation, the multithread GPUs with the CUDA language functionality allow creating of software simulating that kind of fields processing numbers of space/time discrete points only restricted by the GPU threads capacity.

I. Maxwell Equation in Geometric Algebra to Simulate Computing Device of Analog Computer

An analog computer is generally a type of computing device that uses the continuous variation aspect of physical phenomena to model the problem being solved[1]. One special type of physical phenomenon to model problems is considered below.

The circular polarized electromagnetic waves following from the solution of Maxwell equations in free space done in geometric algebra terms,[2], [3],are the electromagnetic fields of the form:

$$F = F_0 exp[I_S(\omega t - k \cdot r)] \qquad (1.1)$$

which should be the solution of

$$(\partial_t + \nabla)F = 0 \qquad (1.2)$$

Solution of (1.2) must be the sum of a vector (electric field e) and bivector (magnetic field $I_3 h$):

Author: [1]Website: https://soiguine.com. e-mail: alex@soiguine.com

$$F = e + I_3 h,$$

with some initial conditions:

$$e + I_3 h|_{t=0,\vec{r}=0} = F_0 = e|_{t=0,\vec{r}=0} + I_3 h|_{t=0,\vec{r}=0} = e_0 + I_3 h_0$$

For a given plane S in (1.1), the solution of the three-dimensional Maxwell equation (1.2) has two options:

- $F_+ = (e_0 + I_3 h_0) exp[I_S(\omega t - k_+ \cdot r)]$, with $\hat{k}_+ = I_3 I_S$, $\hat{e}\hat{h}\hat{k}_+ = I_3$, and the triple $\{\hat{e}, \hat{h}, \hat{k}_+\}$ is right hand screw oriented, that's rotation of $\hat{e}$ to $\hat{h}$ by $\pi/2$ gives movement of *right hand screw* in the direction of $k_+ = |k|I_3 I_S$;

- $F_- = (e_0 + I_3 h_0) exp[I_S(\omega t - k_- \cdot r)]$, with $\hat{k}_- = -I_3 I_S$, $\hat{e}\hat{h}\hat{k}_- = -I_3$, and the triple $\{\hat{e}, \hat{h}, \hat{k}_-\}$ is left hand screw oriented, that's the rotation of $\hat{e}$ to $\hat{h}$ by $\pi/2$ gives movement of *left-hand screw* in the direction of $k_- = -|k|I_3 I_S$ or, equivalently, movement of *right-hand screw* in the opposite direction, $-k_-$;

where e_0 and h_0, initial values of e and h, are arbitrary mutually orthogonal vectors of equal length, lying on the plane S. Vectors $k_\pm = \pm|k_\pm|I_3 I_S$ are normal to that plane. The length of the "wave vectors" $|k_\pm|$ is equal to angular frequency ω.

Maxwell's equation (1.2) is a linear one. Then, any linear combination of F_+ and F_- saving the structure of (1.1) will also be a solution.
Let's write:

$$\begin{cases} F_+ = (e_0 + I_3 h_0) exp[I_S \omega (t - (I_3 I_S) \cdot r)] = (e_0 + I_3 h_0) exp[I_S \omega t] exp[-I_S[(I_3 I_S) \cdot r]] \\ F_- = (e_0 + I_3 h_0) exp[I_S \omega (t + (I_3 I_S) \cdot r)] = (e_0 + I_3 h_0) exp[I_S \omega t] exp[I_S[(I_3 I_S) \cdot r]] \end{cases} \quad (1.3)$$

Then, for arbitrary (real[2]) scalars λ and μ:

$$\lambda F_+ + \mu F_- = (e_0 + I_3 h_0) e^{I_S \omega t} \left(\lambda e^{-I_S[(I_3 I_S) \cdot r]} + \mu e^{I_S[(I_3 I_S) \cdot r]} \right) \quad (1.4)$$

is also solution of (1.2). The item in the second parenthesis is a weighted linear combination of two states (wave functions, g-qubits[4], [5]) with the same phase in the same plane but the opposite sense of orientation. The states are strictly coupled, entangled if you prefer, because the bivector plane should be the same for both, no matter what happens with that plane.
Arbitrary linear combination (1.4) can be rewritten as:

$$\lambda e^{I^+_{Plane} \varphi^+} + \mu e^{I^-_{Plane} \varphi^-} \quad (1.5),$$

with

$$\varphi^\pm = \cos^{-1}\left(\frac{1}{\sqrt{2}} \cos \omega (t \mp [(I_3 I_S) \cdot r]) \right),$$

---

[2] Remember, in the current theory scalars are real ones. "Complex" scalars have no sense.

R_{ef}

4. A. Soiguine, Geometric Phase in Geometric Algebra Qubit Formalism, Saarbrucken: LAMBERT Academic Publishing, 2015.

$$I_{Plane}^{\pm} = I_S \frac{sin\omega(t \mp [(I_3 I_S) \cdot r])}{\sqrt{1 + sin^2\omega(t \mp [(I_3 I_S) \cdot r])}} + I_{B_0} \frac{cos\omega(t \mp [(I_3 I_S) \cdot r])}{\sqrt{1 + sin^2\omega(t \mp [(I_3 I_S) \cdot r])}}$$

$$+ I_{E_0} \frac{sin\omega(t \mp [(I_3 I_S) \cdot r])}{\sqrt{1 + sin^2\omega(t \mp [(I_3 I_S) \cdot r])}}$$

The triple of unit value basis orthonormal bivectors $\{I_S, I_{B_0}, I_{E_0}\}$ comprises the I_S bivector, dual to the propagation direction vector; I_{B_0} is dual to the initial vector of magnetic field; I_{E_0} is dual to the initial vector of electric field. The expression (1.5) is a linear combination of two geometric algebra states, g-qubits.

Linear combination of the two equally weighted solutions of the Maxwell equation F_+ and F_-, $\lambda F_+ + \mu F_-$ with $\lambda = \mu = 1$ reads:

$$\lambda F_+ + \mu F_-|_{\lambda=\mu=1} = 2\cos\omega[(I_3 I_S) \cdot r]\left(\frac{1}{\sqrt{2}}\cos\omega t + I_S \frac{1}{\sqrt{2}}\sin\omega t + I_{B_0} \frac{1}{\sqrt{2}}\cos\omega t + I_{E_0} \frac{1}{\sqrt{2}}\sin\omega t\right)$$

$$(1.6)$$

where $\cos\varphi = \frac{1}{\sqrt{2}}\cos\omega t$ and $\sin\varphi = \frac{1}{\sqrt{2}}\sqrt{1 + (\sin\omega t)^2}$. It can be written in standard exponential form $\cos\varphi + \sin\varphi\, I_B = e^{I_B \varphi}$.[3]

I will call such kind of g-qubits *spreons* (or sprefields.) They spread over the entire three-dimensional space for all values of time and, particularly, instantly change under Clifford translations over the whole three-dimensional space for all values of time, along with the results of measurement of any observable.

II.   CUDA GPU SIMULATION OF THE ANALOG MODELING COMPUTER

In classical mechanics, states are identified by vectors in three-dimensional space [6]. *Infinitesimal transformation of a state, vector, in classical mechanics is:*

$$\vec{X}(t + \Delta t) \approx \vec{X}(t) + \frac{\partial}{\partial t}\vec{X}(t)\Delta t$$

$$\frac{\vec{X}(t + \Delta t) - \vec{X}(t)}{\Delta t} \approx \frac{\partial}{\partial t}\vec{X}(t)$$

In our torsion mechanics [7] states, wave functions, are identified by points on three-sphere $\mathbb{S}^3$. A state[4] there is, see[5], Sec.2.5:

$$e^{I_S(t)\varphi(t)},$$

where I_S is a unit value bivector.

---

[3] Good to remember that the two solutions F_+ and F_- differ only by the sign of $I_3 I_S$, which is caused by the orientation of I_S that, in its turn, defines if the triple $\{\hat{E}, \hat{H}, \pm I_3 I_S\}$ is right-hand screw or left-hand screw oriented.

[4] "State" and "wave function" are synonyms in the current formalism and particular one is used when it is necessary to stress the meaning.

Ref

7. A. Soiguine, The Torsion Mechanics, LAMBERT Academic Publishing, 2023.

If we take a Hamiltonian $H(t) = \alpha + I_3(\beta B_1 + \gamma B_2 + \delta B_3)$ in some orthogonal bivector basis, see[2], then for infinitesimal transformation we have:

$$e^{I_S(t_0+\Delta t)\varphi(t_0+\Delta t)} = e^{-I_H(t_0)|H(t_0)|\Delta t}e^{I_S(t_0)\varphi(t_0)}$$

and

$$\lim_{\Delta t \to 0}\frac{\Delta e^{I_S(t_0)\varphi(t_0)}}{\Delta t} = \lim_{\Delta t \to 0}\frac{e^{I_S(t_0+\Delta t)\varphi(t_0+\Delta t)} - e^{I_S(t_0)\varphi(t_0)}}{\Delta t}$$

$$= \lim_{\Delta t \to 0}\frac{(1 - I_H(t_0)|H(t_0)|\Delta t)e^{I_S(t_0)\varphi(t_0)} - e^{I_S(t_0)\varphi(t_0)}}{\Delta t}$$

$$= -I_H(t_0)|H(t_0)|e^{I_S(t_0)\varphi(t_0)}$$

We received the Schrodinger equation for the state $e^{I_S(t)\varphi(t)}$. That means that the Schrodinger equation governs the evolution of operators, states, which act on observables.

While in classical mechanics, measurement of observable $\vec{x}(t)$ (action by a state) is a shift by a state:

$$\vec{x}(t) \to \vec{x}(t) + \vec{X}(t),$$

in the torsion mechanics it is:

$$C \to e^{-I_S(t)\varphi(t)}Ce^{I_S(t)\varphi(t)},$$

that's rotation in the plane of bivector I_S by angle φ.

Take the general case of observable as a g-qubit: $C = C_0 + C_1B_1 + C_2B_2 + C_3B_3$.

Its measurement by a state $\alpha + \beta_1B_1 + \beta_2B_2 + \beta_3B_3$ is [4]:

$$C_0 + C_1B_1 + C_2B_2 + C_3B_3 \xrightarrow{\alpha+\beta_1B_1+\beta_2B_2+\beta_3B_3} C_0:$$

$$+ \big(C_1[(\alpha^2 + \beta_1^2) - (\beta_2^2 + \beta_3^2)] + 2C_2(\beta_1\beta_2 - \alpha\beta_3) + 2C_3(\alpha\beta_2 + \beta_1\beta_3)\big)B_1$$

$$+ \big(2C_1(\alpha\beta_3 + \beta_1\beta_2) + C_2[(\alpha^2 + \beta_2^2) - (\beta_1^2 + \beta_3^2)] + 2C_3(\beta_2\beta_3 - \alpha\beta_1)\big)B_2$$

$$+ \big(2C_1(\beta_1\beta_3 - \alpha\beta_2) + 2C_2(\alpha\beta_1 + \beta_2\beta_3) + C_3[(\alpha^2 + \beta_3^2) - (\beta_1^2 + \beta_2^2)]\big)B_3$$

When the state is (1.6) we have:

$$B_1 = I_S, \quad B_2 = I_{B_0}, \quad B_3 = I_{E_0}, \quad \alpha = 2\cos\omega[(I_3I_S)\cdot r]\frac{1}{\sqrt{2}}\cos\omega t, \quad \beta_1 = 2\cos\omega[(I_3I_S)\cdot$$

$$r]\frac{1}{\sqrt{2}}\sin\omega t, \beta_2 = 2\cos\omega[(I_3I_S)\cdot r]\frac{1}{\sqrt{2}}\cos\omega t, \beta_3 = 2\cos\omega[(I_3I_S)\cdot r]\frac{1}{\sqrt{2}}\sin\omega t$$

2. A. Soiguine, "Instantaneous Spreading of the g-Qubit Fields," *Journal of Applied Mathematics and Physics*, vol. 7, pp. 591-602, 2019.

Ref

And the measurement result is G_3^+ element spreading through the three-dimensional space for all values of time parameter t:

$$4cos^2\omega[(I_3I_S)\cdot r]\big[C_0 + C_3I_S + (C_1\sin 2\omega t + C_2\cos 2\omega t)I_{B_0} + (C_2\sin 2\omega t - C_1\cos 2\omega t)I_{E_0}\big] \quad (2.1)$$

Geometrically, that means that the measured observable is rotated by $\frac{\pi}{2}$ in the I_{B_0} plane, such that the C_3I_S component becomes orthogonal to plane I_S and remains unchanged. Two other components became orthogonal to I_{B_0} and I_{E_0} and continue rotating in I_S with angular velocity $2\omega t$. The factor $4cos^2\omega[(I_3I_S)\cdot r]$ defines the dependency of that transformed values through all points of the three-dimensional space.

The hardware creating sprefields may require special implementation as a photonic/laser device that does not exist yet. Instead, we have a very convenient equivalent simulation scheme where the amount of simultaneously available space/time points of observable measured values is only restricted by the overall available Nvidia GPU number of threads.

The case of measuring $C = C_0 + C_1B_1 + C_2B_2 + C_3B_3$ by the sprefield is processed by using the following kernel function in the CUDA code:

```
__global__ void quant Kernel(float4* output, int dimx, int dimy, int dimz, float t)

{

float C1 = 1.0//optional components of the observable
float C2 = 1.0;
float C3 = 1.0;
float omega = 12560000.0;              // variant of angular velocity in the sprefield
float tstep = 1.0f;

float factor = 0.0;

    int qidx = threadIdx.x + blockIdx.x * blockDim.x;
int qidy = threadIdx.y + blockIdx.y * blockDim.y;
int qidz = threadIdx.z + blockIdx.z * blockDim.z;

size_t oidx = qidx + qidy*dimx + qidz*dimx*dimy;

  output[oidx][0] = oidx*tstep;
  factor =4*(cosf(omega * output[oidx][0])) * (cosf(omega * output[oidx][0]));
output[oidx][0] += factor * C3;
output[oidx][1] = oidx*tstep;
  output[oidx][1] += factor * (C1 sin(2 * omega * t) + C2 cos(2 * omega * t));
  output[oidx][2] = oidx*tstep;
  output[oidx][2] += factor * (C2 sin(2 * omega * t) - C1 cos(2 * omega * t));
output[oidx][3] =factor;

}
```

More flexibility can be achieved by scattering the sprefield wave function before applying it to observables.

Arbitrary Clifford translation $e^{I_B c^{\gamma}} = \cos\gamma + \sin\gamma\left(\gamma_1 I_S + \gamma_2 I_{B_0} + \gamma_3 I_{E_0}\right)$ acting on spreons (1.6) gives:

$$2\cos\omega[(I_3 I_S)\cdot r]\left[\frac{1}{\sqrt{2}}(\cos\gamma\cos\omega t - \gamma_1\sin\gamma\sin\omega t - \gamma_2\sin\gamma\cos\omega t - \gamma_3\sin\gamma\sin\omega t) + \right.$$

$$\frac{1}{\sqrt{2}}(\cos\gamma\sin\omega t + \gamma_1\sin\gamma\cos\omega t - \gamma_2\sin\gamma\sin\omega t + \gamma_3\sin\gamma\cos\omega t)I_S +$$

$$\frac{1}{\sqrt{2}}(\cos\gamma\cos\omega t + \gamma_1\sin\gamma\sin\omega t + \gamma_2\sin\gamma\cos\omega t - \gamma_3\sin\gamma\sin\omega t)I_{B_0} +$$

$$\left.\frac{1}{\sqrt{2}}(\cos\gamma\sin\omega t - \gamma_1\sin\gamma\cos\omega t + \gamma_2\sin\gamma\sin\omega t + \gamma_3\sin\gamma\cos\omega t)I_{E_0}\right] \tag{2.2}$$

This result is defined for all values of t and r, in other words, the effect of Clifford translation instantly spreads through the whole three dimensions for all values of the time.

The instant of time when the Clifford translation was applied makes no difference for the state (2.2) because it is simultaneously redefined for all values of t. The values of measurements $O\left(C_0, C_1, C_2, C_3, I_S, I_{B_0}, I_{E_0}, \gamma, \gamma_1, \gamma_2, \gamma_3, \omega, t, r\right)$ also get instantly changed for all values of time of measurement, even if the Clifford translation was applied later than the measurement. That is an obvious demonstration that the suggested theory allows indefinite event casual order. In that way, the very notion of the concept of cause and effect, ordered by time value increasing, disappears.

The result of the measurement in general case is a bit tedious. Let us take as an example the bivector components with $\gamma_2 = 1$, $\gamma_1 = \gamma_3 = 0$.

In that case, the result of measurement of $C_0 + C_1 I_S + C_2 I_{B_0} + C_3 I_{E_0}$ can be calculated as its measurement by $\cos\gamma + \sin\gamma I_{B_0}$:

$$C_0 + C_1 I_S + C_2 I_{B_0} + C_3 I_{E_0} \xrightarrow{\cos\gamma + \sin\gamma I_{B_0}} C_0 + (C_1\cos 2\gamma + C_3\sin 2\gamma)I_S + C_2 I_{B_0} + (C_3\cos 2\gamma - C_1\sin 2\gamma)I_{E_0}$$

followed by measurement by

$$2\cos\omega([(I_3 I_S)\cdot\vec{r}])\left(\frac{1}{\sqrt{2}}\cos\omega t + \frac{1}{\sqrt{2}}I_S\sin\omega t + \frac{1}{\sqrt{2}}I_{B_0}\cos\omega t + \frac{1}{\sqrt{2}}I_{E_0}\sin\omega t\right) \text{ that gives:}$$

$$4(\cos\omega\,[(I_3 I_S)\cdot\vec{r}])^2\left[C_0 + (C_3\cos 2\gamma - C_1\sin 2\gamma)\left(\cos 2\gamma\, I_S - \sin 2\gamma\, I_{E_0}\right)\right.$$

$$+ \left((C_1\cos 2\gamma + C_3\sin 2\gamma)\sin 2\omega t + C_2\cos 2\omega t\right)I_{B_0}$$

$$\left. + (C_2\sin 2\omega t - (C_1\cos 2\gamma + C_3\sin 2\gamma)\cos 2\omega t)\left(\cos 2\gamma\, I_{E_0} + \sin 2\gamma\, I_S\right)\right]$$

If we take the new orthonormal bivector basis:

$$\left\{\cos 2\gamma\, I_S - \sin 2\gamma\, I_{E_0}, \sin 2\gamma\, I_S + \cos 2\gamma\, I_{E_0}, \quad I_{B_0}\right\} \equiv \left\{I_{1\gamma}, I_{2\gamma}, I_{B_0}\right\}$$

the result of the measurement reads:

$$4(cos\,\omega\,[(I_3I_S)\cdot\vec{r}])^2\big[C_0 + (C_3\cos 2\gamma - C_1\sin 2\gamma)I_{1\gamma}$$

$$+ \big((C_1\cos 2\gamma + C_3\sin 2\gamma)\sin 2\omega t + C_2\cos 2\omega t\big)I_{B_0}$$

$$+ (C_2\sin 2\omega t - (C_1\cos 2\gamma + C_3\sin 2\gamma)\cos 2\omega t)I_{2\gamma}\big]$$

that has constant value in plane $I_{1\gamma}$ plus rotation in planes I_{B_0} and $I_{2\gamma}$ with angular velocity 2ω.

In that way, we can get an $\vec{r}$-dependent variety of constant components of the results of measurements:

$$4(cos\,\omega\,[(I_3I_S)\cdot\vec{r}])^2\big[C_0 + (C_3\cos 2\gamma - C_1\sin 2\gamma)\big(\cos 2\gamma\,I_S - \sin 2\gamma\,I_{E_0}\big)\big]$$

III. EXAMPLES OF APPLICATIONS OF THE GPU SIMULATING QUANTUM COMPUTER

a) Circulation of flow of a fluid

Assume that fluid in 3D is a field of point-dependent values of vector field $\vec{v}(P)$. Consider a volume element τ containing within it a point P, and denote the bounding surface of τ by σ. Then, the flux of $\vec{v}$ over σ per unit volume is

$$\frac{\int \vec{v}\cdot\vec{n}d\sigma}{\tau}$$

where the integral is taken over the surface σ and $\vec{n}$ is the exterior unit normal to σ. Similarly, we can define:

$$curl\,\vec{v}(P) = \lim_{\tau\to 0}\frac{\int \vec{v}\times\vec{n}d\sigma}{\tau}$$

Let C is simple closed curve bounding a plane area A. At a given point P of A construct unit normal $\vec{v}$ so directed that $\vec{v}$ points in the direction of an advancing right-hand screw when C is traversed in the positive sense.

Take τ as a cylinder with base A and a small height parallel to $\vec{v}$. The cylinder surface is σ. The definition of $curl\,\vec{v}(P)$ yields:

$$\vec{v}\cdot curl\,\vec{v}(P) = \lim_{\tau\to 0}\frac{\int \vec{v}\cdot\vec{v}\times\vec{n}d\sigma}{\tau} = \lim_{A\to 0}\frac{\int \vec{v}\cdot d\vec{r}}{A}$$

where the second integral is along the curve C, and $d\vec{r}$ is the differential of the position vector on C.

The line integral $\int \vec{v}\cdot d\vec{r}$ is called the circulation of $\vec{v}$ along C.

If $\vec{v}$ represents the velocity of a fluid, then $\vec{v}\cdot d\vec{r}$ takes account of the tangential component of velocity $\vec{v}$ and, a fluid particle moving with this velocity circulates along C. A particle moving with velocity $\vec{v}\cdot\vec{n}$ normal to C, on the other hand, crosses C. That

7

Notes

is, it flows either into or out of the region bounded by C. Hence $\vec{v} \cdot curl\ \vec{v}(P)$ provides a measure of the circulation per unit area at point P.

Suppose a fluid is given in a three-dimensional region by continuously differential vector field $\vec{v}(P)$, the fluid velocity. At every point P we have a value $curl\ \vec{v}(P)$ that can be identified by $C = C_0 + C_1 B_1 + C_2 B_2 + C_3 B_3 \equiv Re^{I_S(t)\varphi(t)}$ with geometrically known entities[2]-[5]. The $curl\ \vec{v}(P)$ is the infinitesimal volume density of the net vector circulation, that is magnitude and spatial orientation of the field around the point.

Let us apply the spreon (1.6) to the $curl\ \vec{v}(P)$ at some point P. According to (2.1), the result is:

$$4Rcos^2\omega[(I_3 I_S) \cdot r][C_0 + C_3 I_S + (C_1 \sin 2\omega t + C_2 \cos 2\omega t)I_{B_0}$$
$$+ (C_2 \sin 2\omega t - C_1 \cos 2\omega t)I_{E_0}]$$

In the current scheme any number of test observables can be placed into the continuum of the $(t, \vec{r})$ dependent values of the spreon state, thus fetching out any amount of values $O(C_0, C_1, C_2, C_3, I_S, I_{B_0}, I_{E_0}, \gamma, \gamma_1, \gamma_2, \gamma_3, \omega, t, r)$ spread over three-dimensions and at all instants of time not generally following cause/effect ordering[8].

While the Schrodinger equation governs infinitesimal transformations of a wave function by Clifford translations, a finite Clifford translation moves a wave function along a big circle of $\mathbb{S}^3$ by any Clifford parameter.

In G_3^+ multiplication is:

$$g_1 g_2 = (\alpha_1 + I_{S_1}\beta_1)(\alpha_2 + I_{S_2}\beta_2) = \alpha_1\alpha_2 + I_{S_1}\alpha_2\beta_1 + I_{S_2}\alpha_1\beta_2 + I_{S_1}I_{S_2}\beta_1\beta_2$$

It is not commutative due to the not commutative product of bivectors $I_{S_1}I_{S_2}$. Indeed, taking vectors to which I_{S_1} and I_{S_2} are dual: $s_1 = -I_3 I_{S_1}$, $s_2 = -I_3 I_{S_2}$, we have:

$$I_{S_1}I_{S_2} = -s_1 \cdot s_2 - I_3(s_1 \times s_2)$$

Then:

$$g_1 g_2 = \alpha_1\alpha_2 - (s_1 \cdot s_2)\beta_1\beta_2 + I_{S_1}\alpha_2\beta_1 + I_{S_2}\alpha_1\beta_2 - I_3(s_1 \times s_2)\beta_1\beta_2$$

and

$$g_2 g_1 = \alpha_1\alpha_2 - (s_1 \cdot s_2)\beta_1\beta_2 + I_{S_1}\alpha_2\beta_1 + I_{S_2}\alpha_1\beta_2 + I_3(s_1 \times s_2)\beta_1\beta_2$$

I the case when both elements are of exponent form:

$$e^{I_{S_1}\varphi_1} = \alpha_1 + I_{S_1}\beta_1 = \alpha_1 + \beta_1 b_1^1 B_1 + \beta_1 b_1^2 B_2 + \beta_1 b_1^3 B_3$$

$$e^{I_{S_2}\varphi_2} = \alpha_2 + I_{S_2}\beta_2 = \alpha_2 + \beta_2 b_2^1 B_1 + \beta_2 b_2^2 B_2 + \beta_2 b_2^3 B_3,$$

2. A. Soiguine, "Instantaneous Spreading of the g-Qubit Fields," *Journal of Applied Mathematics and Physics*, vol. 7, pp. 591-602, 2019.

with

$$(\alpha_1)^2 + (\beta_1)^2((b_1^1)^2 + (b_1^2)^2 + (b_1^3)^2) = (\alpha_1)^2 + (\beta_1)^2 = 1$$

$$(\alpha_2)^2 + (\beta_2)^2((b_2^1)^2 + (b_2^2)^2 + (b_2^3)^2) = (\alpha_2)^2 + (\beta_2)^2 = 1,$$

as in the case of a wave function and Clifford translation, we get:

$$e^{Is_2\varphi_2}e^{Is_1\varphi_1} = \cos\varphi_1\cos\varphi_2 + (s_1 \cdot s_2)\sin\varphi_1\sin\varphi_2 + I_3 s_2\cos\varphi_1\sin\varphi_2 + I_3 s_1\cos\varphi_2\sin\varphi_1$$
$$- I_3(s_2 \times s_1)\sin\varphi_1\sin\varphi_2$$

Then it follows that two wave functions are, in any case, connected by the Clifford translation:

$$e^{Is_2\varphi_2} = (e^{Is_2\varphi_2}e^{-Is_1\varphi_1})e^{Is_1\varphi_1} \equiv Cl(S_2,\varphi_2,S_1,\varphi_1)e^{Is_1\varphi_1},$$

where

$$Cl(S_2,\varphi_2,S_1,\varphi_1) \equiv e^{Is_2\varphi_2}e^{-Is_1\varphi_1} = \cos\varphi_1\cos\varphi_2 + (s_1 \cdot s_2)\sin\varphi_1\sin\varphi_2 + I_3 s_2\cos\varphi_1\sin\varphi_2 + I_3 s_1\cos\varphi_2\sin\varphi_1 + I_3(s_2 \times s_1)\sin\varphi_1\sin\varphi_2.$$

From knowing Clifford translation connecting any two wave functions as points on $\mathbb{S}^3$, *it follows that the* result of measurement of any observable C by wave function $e^{Is_1\varphi_1}$, for example, $e^{-Is_1\varphi_1}C\,e^{Is_1\varphi_1} \equiv C(S_1,\varphi_1)$, immediately gives the result of (not made) measurement by $e^{Is_2\varphi_2}$:

$$e^{-Is_2\varphi_2}C\,e^{Is_2\varphi_2} = e^{-Is_2\varphi_2}e^{Is_1\varphi_1}e^{-Is_1\varphi_1}Ce^{Is_1\varphi_1}e^{-Is_1\varphi_1}e^{Is_2\varphi_2} = e^{-Is_2\varphi_2}e^{Is_1\varphi_1}\,C(S_1,\varphi_1)e^{-Is_1\varphi_1}e^{Is_2\varphi_2}$$

$$= Cl(S_2,-\varphi_2,S_1,-\varphi_1)C(S_1,\varphi_1)\overline{Cl(S_2,-\varphi_2,S_1,-\varphi_1)}$$

When assuming observables are also identified by points on $\mathbb{S}^3$ *and thus are connected by formulas as the above one, we get that measurements of any amount of observables by arbitrary set of wave functions are simultaneously available.*

b) Application to block chain schemes

Let us briefly consider the basics of how the block chain scheme generally works in the suggested spreon formalism.
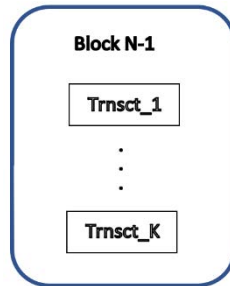
Take a block of transactions stored at some value of time:

The next block is assumed to include transaction Trnsct˙q1 of the part of the measurement result of the observable $C_0 + C_1 B_1 + C_2 B_2 + C_3 B_3$ by the state, that is Clifford translation by $\cos \gamma + I_{B_0} \sin \gamma$ of the spreon

$$2 \cos \omega ([(I_3 I_S) \cdot \vec{r}]) \left(\frac{1}{\sqrt{2}} \cos \omega t + \frac{1}{\sqrt{2}} I_S \sin \omega t + \frac{1}{\sqrt{2}} I_{B_0} \cos \omega t + \frac{1}{\sqrt{2}} I_{E_0} \sin \omega t \right),$$

namely, the part which exists and is constant for all values of time before the transaction and after the transaction. The transaction is a set of elements of G_3^+. The hypothetical quantum channel should transfer sequences of such elements, comprised of factors $4(cos \, \omega \, [(I_3 I_S) \cdot \vec{r_n}])^2$ with predefined values of $\vec{r_n}$ sufficient for enough information about the result of measurement; scalar values C_3 and C_1 of the observable; basis bivectors I_S and I_{E_0}; scalar γ used in creating of a state which acted on the observable, along with the length of wave vector $|k| = \omega$.

Since Trnsct_q1 exists for all values of time it will be automatically included in all previous blocks and in all blocks transacted in the future.
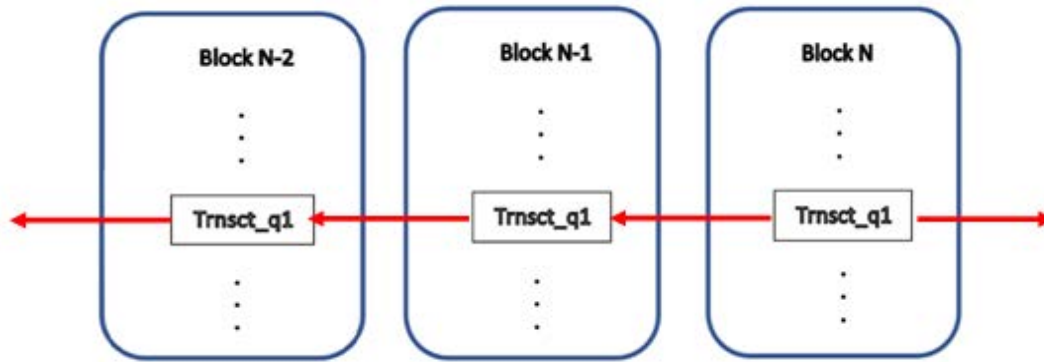
When in future transactions of observable measurement result is transferred, new Trnsct_q2 is placed in all blocks in the same way as above for Trnsct_q1.

IV. CONCLUSIONS

In the suggested theory, all measured observable values get available all together, not through looking one by one. In this way, quantum computer appeared to be a kind of analog computer, keeping and instantly processing information by and on sets of objects possessing an infinite number of degrees of freedom. The multithread GPUs with the CUDA language functionality allow to simultaneously calculate observable measurement values at a number of space/time discrete points, forward and backward in time, the number only restricted by the GPU threads capacity. That eliminates the challenging hardware problem of creating vast and stable arrays of qubits, the basis of quantum computing in conventional approaches.

REFERENCES RÉFÉRENCES REFERENCIAS

1. B. Ulmann, Analog Computing, Oldenbourg: De Gruyter, 2022.
2. A. Soiguine, "Instantaneous Spreading of the g-Qubit Fields," *Journal of Applied Mathematics and Physics*, vol. 7, pp. 591-602, 2019.

Notes

3. A. Soiguine, "Scattering of Geometric Algebra Wave Functions and Collapse in Measurements," *Journal of Applied Matrhematics and Physics*, vol. 8, pp. 1838-1844, 2020.
4. A. Soiguine, Geometric Phase in Geometric Algebra Qubit Formalism, Saarbrucken: LAMBERT Academic Publishing, 2015.
5. A. Soiguine, The Geometric Algebra Lift of Qubits and Beyond, LAMBERT Academic Publishing, 2020. "
6. V. I. Arnold, Mathematical Methods of Classical Mechanics, Springer-Verlag, 1989.
7. A. Soiguine, The Torsion Mechanics, LAMBERT Academic Publishing, 2023.
8. A. Soiguine, "Parallelizable Computing with Geometric Algebra (Alternative to quantum computing based on entanglement)," DOI: 10.13140/RG.2.2.36065.97127, 2019.

N<small>otes</small>